

COIN-OR: Software Tools for Implementing Custom Solvers

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Agenda

- Overview of COIN-OR
- Overview of COIN-OR branch, cut, and price toolbox
 - Introduction to branch, cut, and price algorithms
 - Toolbox components
 - * BCP
 - * OSI
 - * CGL
 - * CLP
 - * VOL
 - The Next Generation
- Using the toolbox
 - Getting started
 - Developing an application
- Examples

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What is COIN-OR?

- The COIN-OR Project

- A **consortium** of researchers in both industry and academia dedicated to improving the state of computational research in OR.
- An **initiative** promoting the development and use of interoperable, open-source software for operations research.
- Soon to become a non-profit corporation known as the COIN-OR Foundation

- The COIN-OR Repository

- A **library** of interoperable software tools for building optimization codes, as well as a few stand alone packages.
- A **venue for peer review** of OR software tools.
- A **development platform** for open source projects, including a CVS repository.

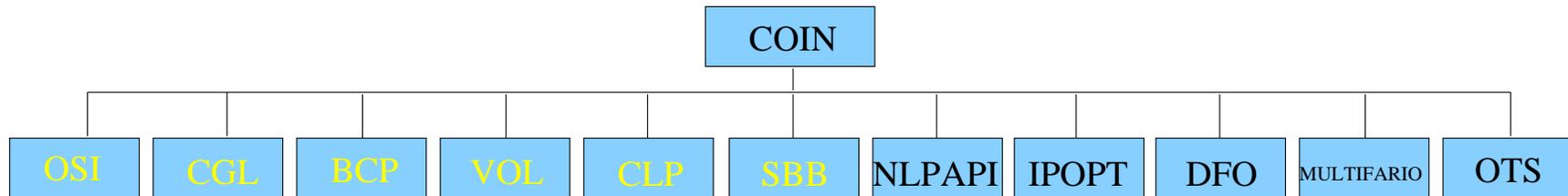
Our Agenda

- Accelerate the pace of research in computational OR.
 - Reuse instead of reinvent.
 - Reduce development time and increase robustness.
 - Increase interoperability (standards and interfaces).
- Provide for software what the open literature provides for theory.
 - Peer review of software.
 - Free distribution of ideas.
 - Adherence to the principles of good scientific research.
- Define standards and interfaces that allow software components to interoperate.
- Increase synergy between various development projects.
- Provide robust, open-source tools for practitioners.

Open Source Development

- *Open source development* is a coding paradigm in which development is done in a cooperative and distributed fashion.
- Strictly speaking, an open source license must satisfy the requirements of the *Open Source Definition*.
- A license cannot call itself “open source” until it is approved by the [Open Source Initiative](#).
- Basic properties of an open source license
 - Access to source code.
 - The right to redistribute.
 - The right to modify.
- The license may require that modifications also be kept open.

Components of the COIN-OR Library



- Branch, cut, price toolbox
 - **OSI**: Open Solver Interface
 - **CGL**: Cut Generator Library
 - **BCP**: Branch, Cut, and Price Library
 - **VOL**: Volume Algorithm
 - **CLP**: COIN-OR LP Solver
 - **SBB**: Simple Branch and Bound
 - **COIN**: COIN-OR Utility Library
- Stand-alone components
 - **IPOPT**: Interior Point Optimization
 - **NLPAPI**: Nonlinear Solver interface
 - **DFO**: Derivative Free Optimization
 - **MULTIFARIO**: Solution Manifolds
 - **OTS**: Open Tabu Search

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Introduction to Branch, Cut, and Price

- Consider problem P :

$$\begin{array}{ll} \min & c^T x \\ \text{s.t.} & Ax \leq b \\ & x_i \in \mathbb{Z} \quad \forall i \in I \end{array}$$

where $A \in \mathbb{R}^{m \times n}$, $b \in \mathbb{R}^m$, $c \in \mathbb{R}^n$.

- Let $\mathcal{P} = \text{conv}\{x \in \mathbb{R}^n : Ax \leq b, x_i \in \mathbb{Z} \forall i \in I\}$.
- Basic Algorithmic Approach
 - Use *LP relaxations* to produce *lower bounds*.
 - *Branch* using hyperplanes.

Branch, Cut, and Price

- Weyl-Minkowski

- $\exists \bar{A} \in \mathbb{R}^{\bar{m} \times n}, \bar{b} \in \mathbb{R}^{\bar{m}}$ s.t. $\mathcal{P} = \{x \in \mathbb{R}^n : \bar{A}x \leq \bar{b}\}$
- We want the solution to $\min\{c^T x : \bar{A}x \leq \bar{b}\}$.
- Solving this LP isn't practical (or necessary).

- BCP Approach

- Form LP relaxations using submatrices of \bar{A} .
- The submatrices are defined by sets $\mathcal{V} \subseteq \{1, \dots, n\}$ and $\mathcal{C} \subseteq \{1, \dots, \bar{m}\}$.
- Forming/managing these relaxations efficiently is one of the primary challenges of BCP.

The Challenge of BCP

- The efficiency of BCP depends heavily on the **size** (number of rows and columns) and **tightness** of the LP relaxations.
- **Tradeoff**
 - Small LP relaxations \Rightarrow **faster LP solution**.
 - Big LP relaxations \Rightarrow **better bounds**.
- The goal is to keep relaxations small while not sacrificing bound quality.
- We must be able to easily move constraints and variables in and out of the **active** set.
- This means dynamic generation and deletion.

An Object-oriented Approach

- The rows/columns of a static LP are called *constraints* and *variables*.
- What do these terms mean in a *dynamic context*?
- Conceptual Definitions
 - Constraint: A mapping that generates coefficients for the *realization* of an inequality for the current set of active variables.
 - Variable: A mapping that generates coefficients corresponding to a variable for the current set of active constraints.
 - Subproblem: Defined by a subset of the global set of variables and constraints.
- To construct a subproblem, an initial *core relaxation* is needed.
- From the core, we can build up other relaxations using the mappings.

Generating the Objects

- We will generically call the constraints and variables *objects*.
- We need to define methods for generating these objects.
- For **constraints**, such a method is a mapping

$$g^c(x) : \mathbb{R}^n \rightarrow 2^{\{1, \dots, \bar{m}\}}$$

where x is a **primal solution** vector.

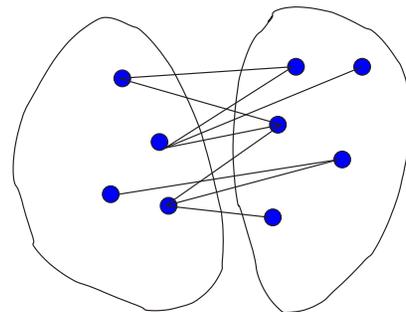
- For **variables**, we have

$$g^v(y) : \mathbb{R}^m \rightarrow 2^{\{1, \dots, n\}}$$

where y is a **dual solution** vector.

Object Representation

- In practice, we may not know the cardinality of the object set.
- We may not easily be able to assign indices to the objects.
- Instead, we must define **abstract representations** of these objects.
- Example: Subtour elimination constraints.



Example: Traveling Salesman Problem

Feasible solutions are those incidence vectors satisfying:

$$\begin{aligned}\sum_{j=1}^n x_{ij} &= 2 \quad \forall i \in V \\ \sum_{\substack{i \in S \\ j \notin S}} x_{ij} &\geq 2 \quad \forall S \subset V, |S| > 1.\end{aligned}$$

- The variables correspond to the edges of a graph (easy to index).
- The number of facets (constraints) is astronomical.
- The core
 - The k shortest edges adjacent to each node.
 - The degree constraints.
- Generate subtour elimination constraints and other variables dynamically.

The COIN-OR Branch, Cut, and Price Toolbox

Branch, cut, price toolbox components

- **COIN**: Collection of utilities.
- **BCP**: Tool for implementing BCP algorithms
- **OSI**: Tool for interfacing to third-party solvers (particularly LP solvers)
- **CGL**: Tool for generating valid inequalities (within BCP)
- **VOL**: Fast approximate LP solver (with OSI interface)
- **CLP**: COIN-OR LP Solver (with OSI interface)
- **SBB**: A lightweight generic MIP solver.

COIN/BCP

- **Concept:** Provide a *framework* in which the user has only to define constraints, variables, and a core.
 - Branch and bound \Rightarrow core only
 - Branch and cut \Rightarrow core plus constraints
 - Branch and price \Rightarrow core plus variables
 - Branch, cut, and price \Rightarrow the whole caboodle
- **Existing BCP frameworks**
 - SYMPHONY (parallel, C)
 - COIN/BCP (parallel, C++)
 - ABACUS (sequential, C++)
- **Tools Needed**
 - Framework
 - LP Solver
 - Cut Generator

OSI Overview

Uniform interface to LP solvers, including:

- [CLP](#) (COIN-OR)
- [CPLEX](#) (ILOG)
- [DyLP](#) (BonsaiG LP Solver)
- [GLPK](#) (GNU LP Kit)
- [OSL](#) (IBM)
- [SoPlex](#) (Konrad-Zuse-Zentrum für Informationstechnik Berlin)
- [Volume](#) (COIN-OR)
- [XPRESS](#) (Dash Optimization)

CGL Overview

- Collection of cut generating methods integrated with OSI.
- Intended to provide robust implementations, including computational tricks not usually published.
- Currently includes:
 - Simple rounding cut
 - Gomory cut
 - Knapsack cover cut
 - Rudimentary lift-and-project cut (covering and packing)
 - Odd hole cut
 - Probing cut

VOL Overview

- Generalized **subgradient** optimization algorithm.
- Compatible with branch, cut, and price:
 - provides approximate **primal and dual solutions**,
 - provides a **valid lower bound** (feasible dual solution), and
 - provides a method for **warm starting**.

CLP Overview

- A full-featured, open source LP solver.
- Has interfaces for primal, dual, and network simplex.
- Can be accessed through the OSI.
- Reasonably robust and fast.

SBB

- A lightweight generic MIP solver.
- Uses **OSI** to solve the LP relaxations.
- Uses **CGL** to generate cuts.
- Optimized for **CLP**.

COIN Utility Library

- Contains classes for
 - Storage and manipulation of sparse vectors and matrices.
 - Factorization of sparse matrices.
 - Storage of solver warm start information.
 - Message handling.
 - Reading/writing of MPS files.
 - Other utilities (simultaneous sorting, timing, ...).
- These are the classes common to many of the other algorithms.

OSI Redesign

- We are redesigning the OSI in conjunction with the development of BiCePS.
- Design goals
 - Ability to handle a wider variety of models (linear, nonlinear, integer).
 - Ability to interface with a wider variety of solvers.
- Design overview
 - The `OsiModel` class consists of a collection of
 - * `OsiConstraints`, and
 - * `OsiVariables`,each of which have an associated `OsiDomain`.
- The `OsiAlgorithm` class describes the interface for a particular algorithm, such as
 - `OsiAlgorithmSimplex`, or
 - `OsiAlgorithmBarrier`.
- Once a model is built, it can be attached to an algorithm class.

The ALPS Project

- In partnership with IBM and the COIN-OR project.
- Multi-layered C++ class library for implementing scalable, parallel tree search algorithms.
- Design is fully generic and portable.
 - Support for implementing general **tree search algorithms**.
 - Support for any **bounding** scheme.
 - **No assumptions** on problem/algorithm type.
 - No dependence on **architecture/operating system**.
 - No dependence on **third-party software** (communications, solvers).
- Emphasis on parallel **scalability**.
- Support for large-scale, **data-intensive** applications (such as BCP).
- Support for **advanced methods** not available in commercial codes.
- Will include a layer for implementing BCP algorithms.

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COIN/BCP Overview

- The COIN/BCP library is divided into modules, of which there are four basic types:
 - Master** Maintains problem instance data, spawns other processes, performs I/O, fault tolerance.
 - Tree Manager** Controls overall execution by tracking growth of the tree and dispatching subproblems to the LP solvers.
 - Node Processor** Perform processing and branching operations.
 - Object Generator** Generate objects.
- The division into separate modules makes the code highly configurable and parallelizable.

COIN/BCP Overview: Node Processor

Handling of Constraints

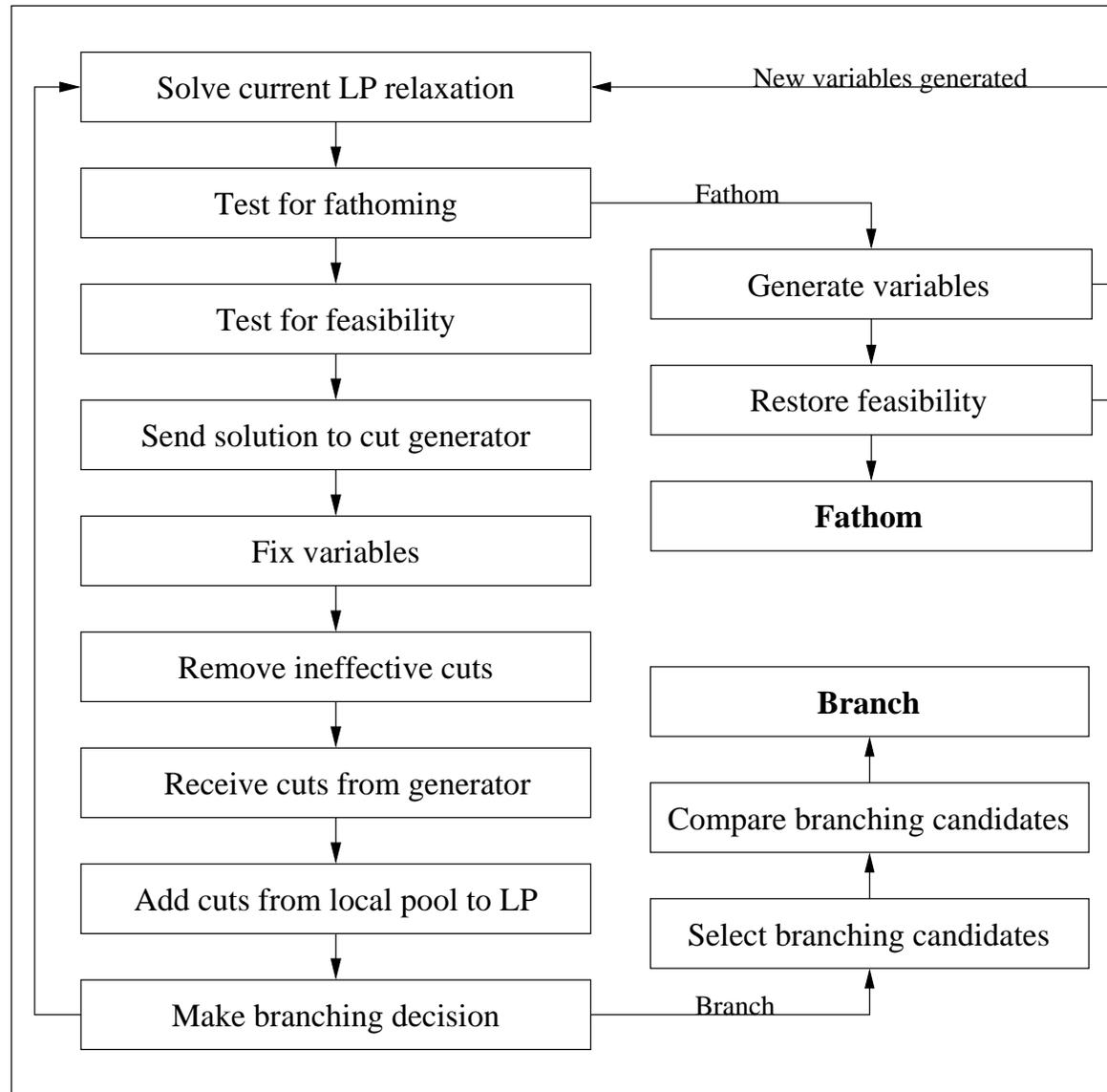
- Cuts are generated by the **cut generators** and/or by the node processor itself.
- Violated cuts are received and processed by the LP modules.
- Each LP module maintains a small **local cut pool**.
- A limited number of cuts are added to the LP relaxations each iteration to prevent “saturation.”
- Ineffective (non-core) cuts are aggressively removed.

COIN/BCP Overview: Node Processor

Handling of Variables

- **Reduced cost/logical fixing** are used to remove (non-core) variables.
- **Variable generation** may be needed for very large problems.
- **Exact generation must take place before fathoming!**
- **Two-phase algorithm**
 - BCP is run to completion on the core variables before generating new ones.
 - Using the upper bound and cuts from the first phase, all variables are **priced out in the root node** and are then propagated down into the leaves as required.
 - The **tree is trimmed** by aggregating children back into their parent.
 - Afterwards, each leaf is processed again.

COIN/BCP Overview: Node Processor Main Loop



Getting the Source Code

- The source can be obtained from www.coin-or.org as “tarball” or using CVS.
- Platforms/Requirements
 - Linux, gcc 2.95.3/2.96RH/3.2/3.3
 - Windows, Visual C++, CygWin make (untested)
 - Sun Solaris, gcc 2.95.3/3.2 or SunWorkshop C++
 - AIX gcc 2.95.3/3.3
 - Mac OS X
- Editing the Makefiles
 - `Makefile.location`
 - `Makefile.<operating system>`
- Make the necessary libraries. They’ll be installed in `${CoinDir}/lib`.
 - Change to appropriate directory and type `make`.

Developing an Application

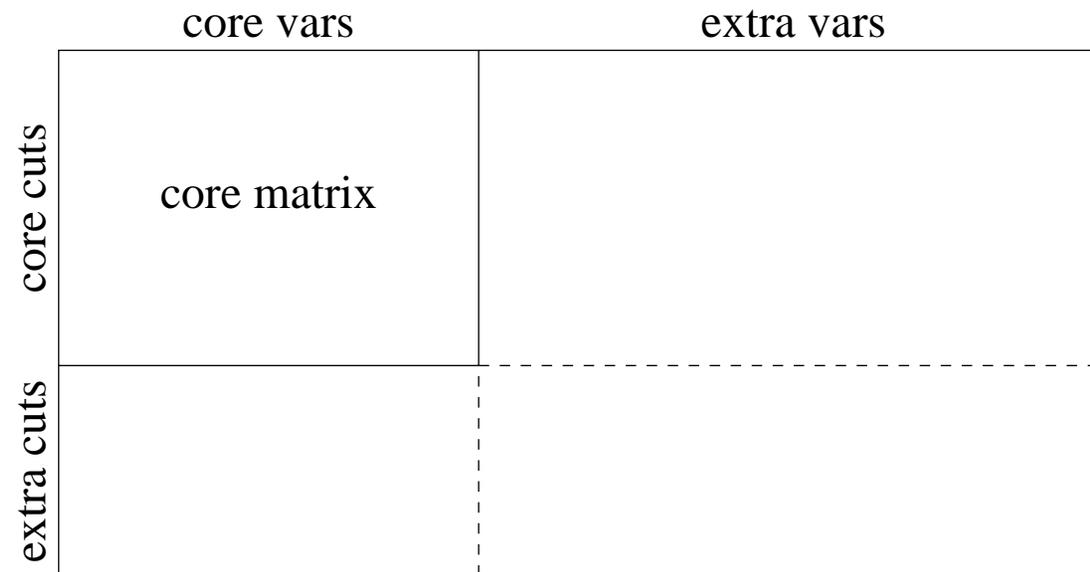
- The user API is implemented via a C++ class hierarchy.
- To develop an application, the user must derive the appropriate classes override the appropriate methods.
- Classes for customizing the behavior of the modules
 - BCP_tm_user
 - BCP_lp_user
 - BCP_cg_user
 - BCP_vg_user
- Classes for defining user objects
 - BCP_cut
 - BCP_var
 - BCP_solution
- Allowing COIN/BCP to create instances of the user classes.
 - The user must derive the class `USER_initialize`.
 - The function `BCP_user_init()` returns an instance of the derived initializer class.

Objects in COIN/BCP

- Most application-specific methods are related to handling of objects.
- Since representation is independent of the current LP, the user must define methods to add objects to a given subproblem.
- For parallel execution, the objects need to be packed into (and unpacked from) a buffer.
- Object Types
 - **Core objects** are objects that are active in every subproblem (`BCP_xxx_core`).
 - **Indexed objects** are extra objects that can be uniquely identified by an index (such as the edges of a graph) (`BCP_xxx_indexed`).
 - **Algorithmic objects** are extra objects that have an abstract representation (`BCP_xxx_algo`).

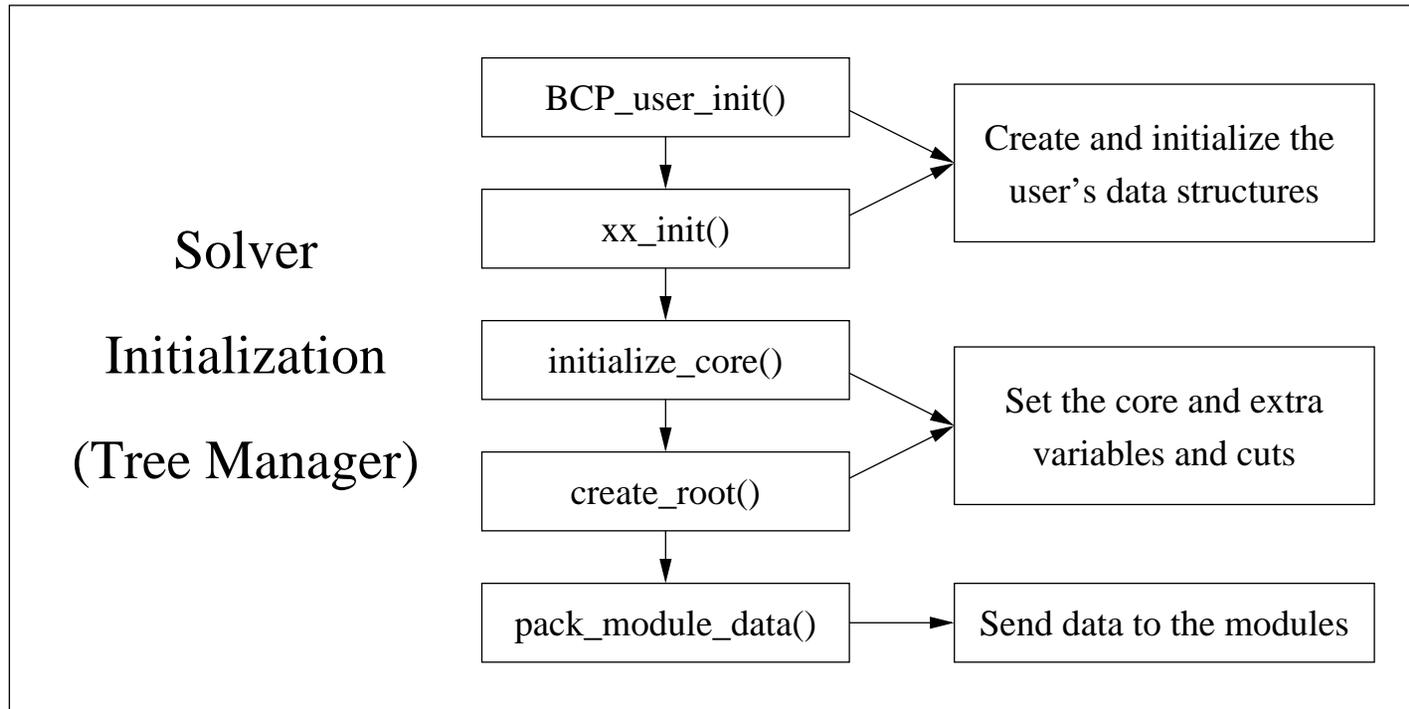
Forming the LP Relaxations in COIN/BCP

The current LP relaxation looks like this:



Reason for this split: efficiency.

COIN/BCP Methods: Initialization



COIN/BCP Methods: Steady State

unpack_feasible_solution()

init_new_phase()

compare_tree_nodes()

Tree Manager

unpack_module_data()

unpack_primal_solution()

generate_cuts()

Cut Generator

unpack_module_data()

initialize_search_tree_node()

See the solver loop figure

LP Solver

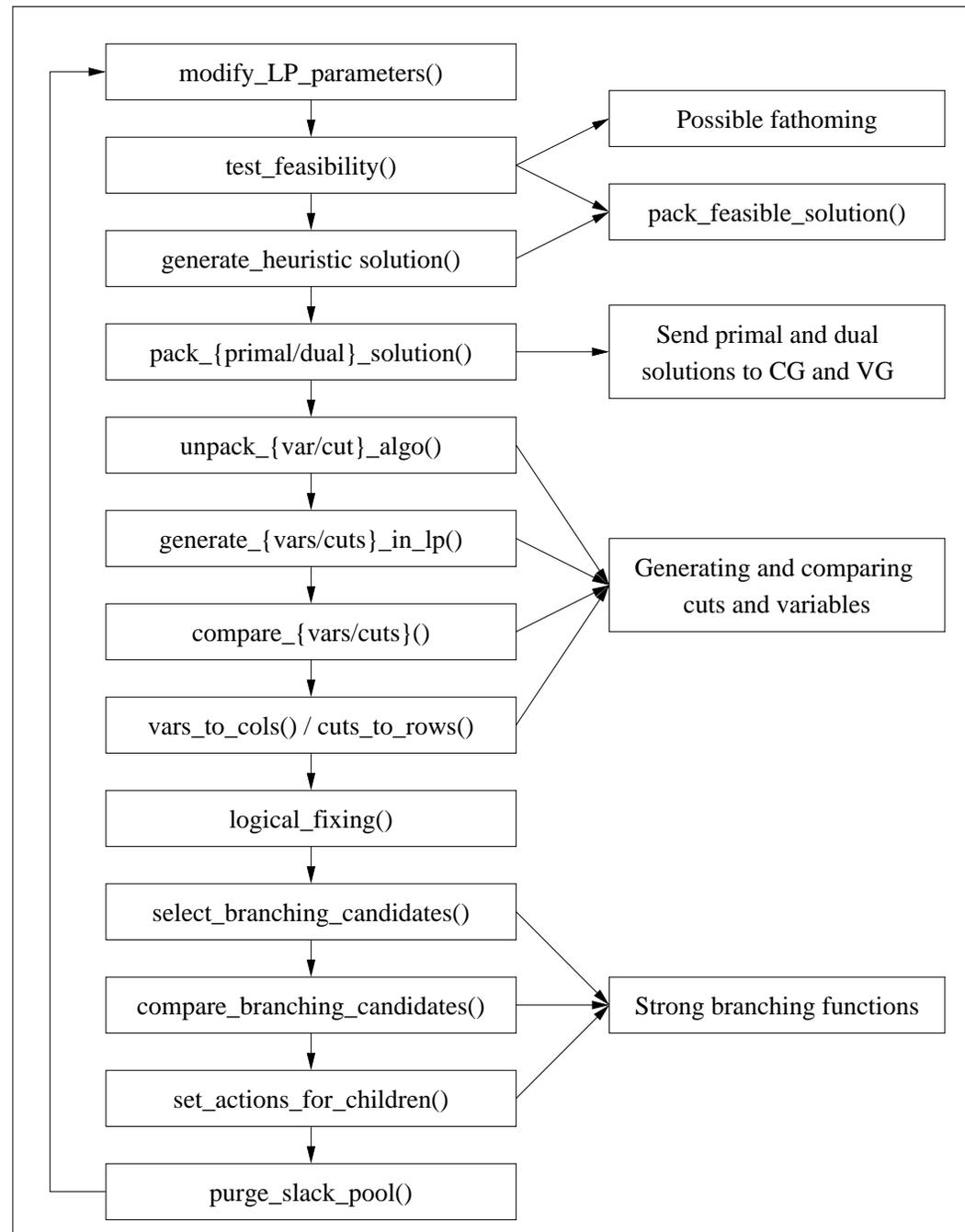
unpack_module_data()

unpack_dual_solution()

generate_vars()

Variable Generator

COIN/BCP Methods: Node Processing Loop



COIN/BCP Methods: Node Processing Loop

Var generation	B&B	Cut generation
<p><code>compute_lower_bound</code></p> <p><code>pack_dual_solution</code></p> <p><code>generate_vars_in_lp</code></p> <p><i>vars are added</i></p>	<p><code>initialize_new_search_tree_node</code></p> <p><code>modify_lp_parameters</code></p> <p><i>solve the LP relaxation</i></p> <p><code>display_lp_solution</code></p> <p><code>test_feasibility</code></p> <p><i>reduced cost fixing</i></p> <p><code>logical_fixing</code></p> <p><code>generate_heuristic_solution</code></p> <p><code>select_branching_candidates</code></p> <p><i>If branching is decided on</i></p> <p><code>compare_branching_candidates</code></p> <p><code>set_actions_for_children</code></p> <p><i>Otherwise</i></p>	<p><code>pack_primal_solution</code></p> <p><code>generate_cuts_in_lp</code></p> <p><i>cuts are added</i></p>

Misc methods in the TM (no particular order)

- `unpack_feasible_solution`. Default: Unpack a generic solution.
Write if own solution type used.
- `display_feasible_solution`. Default: display a generic solution.
Write if own solution type used.
- `(un)pack_warmstart`. Default: handles all warmstarts defined in Osi.
Unlikely to write.
- `(un)pack_var_algo`. Write if algorithmic vars are generated.
- `(un)pack_cut_algo`. Write if algorithmic cuts are generated.
- `compare_tree_nodes`. Defaults: Breadth/Depth/Best First Search.
Unlikely to write (only if none of the defaults are satisfactory).
- `init_new_phase`. Unlikely to write (only if multiphase is used).

Misc methods in the LP (no particular order)

- `pack_feasible_solution`. Invoked whenever a feasible soln is found.
Default: Pack a generic solution.
Write if own solution type used.
- `(un)pack_warmstart`. Default: handles all warmstarts defined in Osi.
Unlikely to write.
- `(un)pack_var_algo`.
Write if algorithmic vars are generated.
- `(un)pack_cut_algo`.
Write if algorithmic cuts are generated.
- `cuts_to_rows` and `vars_to_cols`.
Write if any sort of cut/var generation is done.
- `compare_cuts` and `compare_vars`.
Write if any sort of cut/var generation is done.

Parameters and using the finished code

- Create a parameter file
- Run your code with the parameter file name as an argument (command line switches will be added).
- BCP_ for BCP's parameters
- Defined and documented in `BCP_tm_par`, `BCP_lp_par`, etc.
- Helper class for creating your parameters.
- Output controlled by verbosity parameters.

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Example: Uncapacitated Facility Location

User classes and methods

- **UFL_init**
 - `tm_init()`
 - `lp_init()`
- **UFL_lp**
 - `unpack_module_data()`
 - `pack_cut_algo()`
 - `unpack_cut_algo()`
 - `generate_cuts_in_lp()`
 - `cuts_to_rows()`
- **UFL_tm**
 - `read_data()`
 - `initialize_core()`
 - `pack_module_data()`
- **UFL_cut**

Example: Generic MIP solver

- Implement branch and cut to solve an IP by
 - reading in from an MPS file,
 - designating all vars as core vars,
 - selecting some of the constraints as core constraints
 - making the rest extra (indexed) constraints, and
 - interfacing to CGL to generate cuts.
- Classes and methods are similar to the previous example.

Resources

- Documentation
 - There is a user's manual for BCP, but it is out of date.
 - The most current documentation is in the source code—don't be afraid to use it.
- Other resources
 - There are several mailing lists on which to post questions and we make an effort to answer quickly.
 - Also, there is a lot of good info at www.coin-or.org.
- There will be a user's meeting today from 12-1!

Final advice

Use the source, Luke...

...and feel free to ask questions either by email or on the discussion list.